Package: pense (via r-universe)

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https://github.com/dakep/pense-rpkg

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Description Robust penalized (adaptive) elastic net S and M estimators for linear regression. The methods are proposed in Cohen Freue, G. V., Kepplinger, D., Salibián-Barrera, M., and Smucler, E. (2019) https://projecteuclid.org/euclid.aoas/1574910036>. The package implements the extensions and algorithms described in Kepplinger, D. (2020) <doi:10.14288/1.0392915>.

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cd_algorithm_options Coordinate Descent (CD) Algorithm to Compute Penalized Elastic Net S-estimates

Description

Set options for the CD algorithm to compute adaptive EN S-estimates.

Usage

```
cd_algorithm_options(
  max_it = 1000,
  reset_it = 8,
  linesearch_steps = 4,
  linesearch_mult = 0.5
)
```

Arguments

maximum number of iterations.
number of iterations after which the residuals are re-computed from scratch, to prevent numerical drifts from incremental updates.
os
maximum number of steps used for line search.
t
multiplier to adjust the step size in the line search.

Value

options for the CD algorithm to compute (adaptive) PENSE estimates.

See Also

mm_algorithm_options to optimize the non-convex PENSE objective function via a sequence of convex problems.

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coef.pense_cvfit Extract Coefficient Estimates

Description

Extract coefficients from an adaptive PENSE (or LS-EN) regularization path with hyper-parameters chosen by cross-validation.

Usage

```
## S3 method for class 'pense_cvfit'
coef(
    object,
    alpha = NULL,
    lambda = "min",
    se_mult = 1,
    sparse = NULL,
    standardized = FALSE,
    exact = deprecated(),
    correction = deprecated(),
    ...
)
```

Arguments

object	PENSE with cross-validated hyper-parameters to extract coefficients from.
alpha	Either a single number or NULL (default). If given, only fits with the given alpha value are considered. If lambda is a numeric value and object was fit with multiple <i>alpha</i> values and no value is provided, the first value in object\$alpha is used with a warning.
lambda	either a string specifying which penalty level to use ("min", "se", "{m}-se") or a single numeric value of the penalty parameter. See details.
se_mult	If lambda = "se", the multiple of standard errors to tolerate.
sparse	should coefficients be returned as sparse or dense vectors? Defaults to the spar- sity setting of the given object. Can also be set to sparse = 'matrix', in which case a sparse matrix is returned instead of a sparse vector.
standardized exact, correcti	return the standardized coefficients. on
	defunct.
	currently not used.

Value

either a numeric vector or a sparse vector of type dsparseVector of size p + 1, depending on the sparse argument. Note: prior to version 2.0.0 sparse coefficients were returned as sparse matrix of type dgCMatrix. To get a sparse matrix as in previous versions, use sparse = 'matrix'.

coef.pense_fit

Hyper-parameters

If lambda = "{m}-se" and object contains fitted estimates for every penalization level in the sequence, use the fit the most parsimonious model with prediction performance statistically indistinguishable from the best model. This is determined to be the model with prediction performance within $m \star cv_se$ from the best model. If lambda = "se", the multiplier *m* is taken from se_mult.

By default all *alpha* hyper-parameters available in the fitted object are considered. This can be overridden by supplying one or multiple values in parameter alpha. For example, if lambda = "1-se" and alpha contains two values, the "1-SE" rule is applied individually for each alpha value, and the fit with the better prediction error is considered.

In case lambda is a number and object was fit for several *alpha* hyper-parameters, alpha must also be given, or the first value in object\$alpha is used with a warning.

See Also

Other functions for extracting components: coef.pense_fit(), predict.pense_cvfit(), predict.pense_fit(), residuals.pense_cvfit(), residuals.pense_fit()

Examples

```
# Compute the PENSE regularization path for Freeny's revenue data
# (see ?freeny)
data(freeny)
x <- as.matrix(freeny[ , 2:5])</pre>
regpath <- pense(x, freeny$y, alpha = 0.5)</pre>
plot(regpath)
# Extract the coefficients at a certain penalization level
coef(regpath, lambda = regpath$lambda[[1]][[40]])
# What penalization level leads to good prediction performance?
set.seed(123)
cv_results <- pense_cv(x, freeny$y, alpha = 0.5,</pre>
                       cv_repl = 2, cv_k = 4)
plot(cv_results, se_mult = 1)
# Extract the coefficients at the penalization level with
# smallest prediction error ...
coef(cv_results)
# ... or at the penalization level with prediction error
# statistically indistinguishable from the minimum.
coef(cv_results, lambda = '1-se')
```

coef.pense_fit Extract Coefficient Estimates

Description

Extract coefficients from an adaptive PENSE (or LS-EN) regularization path fitted by pense() or elnet().

Usage

```
## S3 method for class 'pense_fit'
coef(
   object,
   lambda,
   alpha = NULL,
   sparse = NULL,
   standardized = FALSE,
   exact = deprecated(),
   correction = deprecated(),
   ...
)
```

Arguments

object	PENSE regularization path to extract coefficients from.
lambda	a single number for the penalty level.
alpha	Either a single number or NULL (default). If given, only fits with the given alpha value are considered. If object was fit with multiple alpha values, and no value is provided, the first value in object\$alpha is used with a warning.
sparse	should coefficients be returned as sparse or dense vectors? Defaults to the spar- sity setting in object. Can also be set to sparse = 'matrix', in which case a sparse matrix is returned instead of a sparse vector.
standardized	return the standardized coefficients.
exact, correction	
	defunct.
	currently not used.

Value

either a numeric vector or a sparse vector of type dsparse Vector of size p + 1, depending on the sparse argument. Note: prior to version 2.0.0 sparse coefficients were returned as sparse matrix of type dgCMatrix. To get a sparse matrix as in previous versions, use sparse = 'matrix'.

See Also

coef.pense_cvfit() for extracting coefficients from a PENSE fit with hyper-parameters chosen
by cross-validation

Other functions for extracting components: coef.pense_cvfit(), predict.pense_cvfit(), predict.pense_fit(), residuals.pense_cvfit(), residuals.pense_fit()

consistency_const

Examples

```
# Compute the PENSE regularization path for Freeny's revenue data
# (see ?freeny)
data(freeny)
x <- as.matrix(freeny[ , 2:5])</pre>
regpath <- pense(x, freeny$y, alpha = 0.5)</pre>
plot(regpath)
# Extract the coefficients at a certain penalization level
coef(regpath, lambda = regpath$lambda[[1]][[40]])
# What penalization level leads to good prediction performance?
set.seed(123)
cv_results <- pense_cv(x, freeny$y, alpha = 0.5,</pre>
                       cv_repl = 2, cv_k = 4)
plot(cv_results, se_mult = 1)
# Extract the coefficients at the penalization level with
# smallest prediction error ...
coef(cv_results)
# ... or at the penalization level with prediction error
# statistically indistinguishable from the minimum.
coef(cv_results, lambda = '1-se')
```

consistency_const Get the Constant for Consistency for the M-Scale

Description

Get the Constant for Consistency for the M-Scale

Usage

```
consistency_const(delta, rho)
```

Arguments

delta	desired breakdown point (between 0 and 0.5)
rho	the name of the chosen ρ function.

Value

consistency constant

See Also

Other miscellaneous functions: rho_function()

deprecated_en_options Deprecated

Description

[Deprecated]

Options for computing EN estimates.

Usage

```
en_options_aug_lars(use_gram = c("auto", "yes", "no"), eps = 1e-12)
```

```
en_options_dal(
  maxit = 100,
  eps = 1e-08,
  eta_mult = 2,
  eta_start_numerator = 0.01,
  eta_start,
  preconditioner = c("approx", "none", "diagonal"),
  verbosity = 0
)
```

Arguments

use_gram	ignored. Should the Gram matrix be pre-computed.
eps	ignored. Numeric tolerance for convergence.
maxit	maximum number of iterations allowed.
eta_mult	multiplier to increase eta at each iteration.
eta_start_nume	rator
	<pre>if eta_start is missing, it is defined by eta_start = eta_start_numerator / lambda.</pre>
eta_start	ignored. The start value for eta.
preconditioner	ignored. Preconditioner for the numerical solver. If none, a standard solver will be used, otherwise the faster preconditioned conjugate gradient is used.
verbosity	ignored.

Functions

- en_options_aug_lars(): Superseded by en_lars_options().
- en_options_dal(): Superseded by en_dal_options()

Warning

Do not use these functions in new code. They may be removed from future versions of the package.

elnet

See Also

Other deprecated functions: enpy(), initest_options(), mstep_options(), pense_options(), pensem()

elnet

Compute the Least Squares (Adaptive) Elastic Net Regularization Path

Description

Compute least squares EN estimates for linear regression with optional observation weights and penalty loadings.

Usage

```
elnet(
  х,
 у,
  alpha,
 nlambda = 100,
  lambda_min_ratio,
  lambda,
 penalty_loadings,
 weights,
  intercept = TRUE,
  en_algorithm_opts,
  sparse = FALSE,
  eps = 1e-06,
  standardize = TRUE,
  correction = deprecated(),
 xtest = deprecated(),
  options = deprecated()
```

Arguments

)

x	n by p matrix of numeric predictors.
У	vector of response values of length n. For binary classification, y should be a factor with 2 levels.
alpha	elastic net penalty mixing parameter with $0 \le \alpha \le 1$. alpha = 1 is the LASSO penalty, and alpha = 0 the Ridge penalty. Can be a vector of several values, but alpha = 0 cannot be mixed with other values.
nlambda	number of penalization levels.
lambda_min_rat	lo
	Smallest value of the penalization level as a fraction of the largest level (i.e., the smallest value for which all coefficients are zero). The default depends on

	the sample size relative to the number of variables and alpha. If more observations than variables are available, the default is $1e-3 \times alpha$, otherwise $1e-2 \times alpha$.
lambda	optional user-supplied sequence of penalization levels. If given and not NULL, nlambda and lambda_min_ratio are ignored.
penalty_loadin	gs
	a vector of positive penalty loadings (a.k.a. weights) for different penalization of each coefficient.
weights	a vector of positive observation weights.
intercept	include an intercept in the model.
en_algorithm_opts	
	options for the EN algorithm. See en_algorithm_options for details.
sparse	use sparse coefficient vectors.
eps	numerical tolerance.
standardize	standardize variables to have unit variance. Coefficients are always returned in original scale.
correction	defunct. Correction for EN estimates is not supported anymore.
xtest	defunct.
options	deprecated. Use en_algorithm_opts instead.

Details

The elastic net estimator for the linear regression model solves the optimization problem

$$argmin_{\mu,\beta}(1/2n)\sum_{i}w_{i}(y_{i}-\mu-x_{i}'\beta)^{2}+\lambda\sum_{j}0.5(1-\alpha)\beta_{j}^{2}+\alpha l_{j}|\beta_{j}|$$

with observation weights w_i and penalty loadings l_i .

Value

a list-like object with the following items

alpha the sequence of alpha parameters.

lambda a list of sequences of penalization levels, one per alpha parameter.

estimates a list of estimates. Each estimate contains the following information:

intercept intercept estimate.

beta beta (slope) estimate.

lambda penalization level at which the estimate is computed.

alpha *alpha* hyper-parameter at which the estimate is computed.

statuscode if > 0 the algorithm experienced issues when computing the estimate.

status optional status message from the algorithm.

call the original call.

elnet_cv

See Also

pense() for an S-estimate of regression with elastic net penalty.

coef.pense_fit() for extracting coefficient estimates.

plot.pense_fit() for plotting the regularization path.

Other functions for computing non-robust estimates: elnet_cv()

Examples

```
# Compute the LS-EN regularization path for Freeny's revenue data
# (see ?freeny)
data(freeny)
x <- as.matrix(freeny[ , 2:5])</pre>
regpath <- elnet(x, freeny$y, alpha = c(0.5, 0.75))</pre>
plot(regpath)
plot(regpath, alpha = 0.75)
# Extract the coefficients at a certain penalization level
coef(regpath, lambda = regpath$lambda[[1]][[5]],
     alpha = 0.75)
# What penalization level leads to good prediction performance?
set.seed(123)
cv_results <- elnet_cv(x, freeny$y, alpha = c(0.5, 0.75),
                       cv_repl = 10, cv_k = 4,
                       cv_measure = "tau")
plot(cv_results, se_mult = 1.5)
plot(cv_results, se_mult = 1.5, what = "coef.path")
# Extract the coefficients at the penalization level with
# smallest prediction error ...
summary(cv_results)
coef(cv_results)
# ... or at the penalization level with prediction error
# statistically indistinguishable from the minimum.
summary(cv_results, lambda = "1.5-se")
coef(cv_results, lambda = "1.5-se")
```

elnet_cv

Cross-validation for Least-Squares (Adaptive) Elastic Net Estimates

Description

Perform (repeated) K-fold cross-validation for elnet().

Usage

```
elnet_cv(
    x,
    y,
    lambda,
    cv_k,
    cv_repl = 1,
    cv_metric = c("rmspe", "tau_size", "mape", "auroc"),
    fit_all = TRUE,
    cl = NULL,
    ncores = deprecated(),
    ...
)
```

Arguments

x	n by p matrix of numeric predictors.
х У	vector of response values of length n. For binary classification, y should be a factor with 2 levels.
lambda	optional user-supplied sequence of penalization levels. If given and not NULL, nlambda and lambda_min_ratio are ignored.
cv_k	number of folds per cross-validation.
cv_repl	number of cross-validation replications.
cv_metric	either a string specifying the performance metric to use, or a function to eval- uate prediction errors in a single CV replication. If a function, the number of arguments define the data the function receives. If the function takes a single argument, it is called with a single numeric vector of prediction errors. If the function takes two or more arguments, it is called with the predicted values as first argument and the true values as second argument. The function must al- ways return a single numeric value quantifying the prediction performance. The order of the given values corresponds to the order in the input data.
fit_all	If TRUE, fit the model for all penalization levels. Can also be any combination of "min" and " $\{x\}$ -se", in which case only models at the penalization level with smallest average CV accuracy, or within $\{x\}$ standard errors, respectively. Setting fit_all to FALSE is equivalent to "min". Applies to all alpha value.
cl	a parallel cluster. Can only be used in combination with ncores = 1.
ncores	deprecated and not used anymore.
	Arguments passed on to elnet
	 alpha elastic net penalty mixing parameter with 0 ≤ α ≤ 1. alpha = 1 is the LASSO penalty, and alpha = 0 the Ridge penalty. Can be a vector of several values, but alpha = 0 cannot be mixed with other values. nlambda number of penalization levels. lambda_min_ratio Smallest value of the penalization level as a fraction of the largest level (i.e., the smallest value for which all coefficients are zero). The default depends on the sample size relative to the number of variables and

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alpha. If more observations than variables are available, the default is 1e-3 * alpha, otherwise 1e-2 * alpha.

- penalty_loadings a vector of positive penalty loadings (a.k.a. weights) for different penalization of each coefficient.
- standardize standardize variables to have unit variance. Coefficients are always returned in original scale.

weights a vector of positive observation weights.

intercept include an intercept in the model.

sparse use sparse coefficient vectors.

en_algorithm_opts options for the EN algorithm. See en_algorithm_options for details.

eps numerical tolerance.

xtest defunct.

options deprecated. Use en_algorithm_opts instead.

correction defunct. Correction for EN estimates is not supported anymore.

Details

The built-in CV metrics are

"tau_size" τ -size of the prediction error, computed by tau_size() (default).

"mape" Median absolute prediction error.

"rmspe" Root mean squared prediction error.

"auroc" Area under the receiver operator characteristic curve (actually 1 - AUROC). Only sensible for binary responses.

Value

a list-like object with the same components as returned by elnet(), plus the following:

cvres data frame of average cross-validated performance.

See Also

elnet() for computing the LS-EN regularization path without cross-validation.

pense_cv() for cross-validation of S-estimates of regression with elastic net penalty.

coef.pense_cvfit() for extracting coefficient estimates.

plot.pense_cvfit() for plotting the CV performance or the regularization path.

Other functions for computing non-robust estimates: elnet()

Examples

```
# Compute the LS-EN regularization path for Freeny's revenue data
# (see ?freeny)
data(freeny)
x <- as.matrix(freeny[ , 2:5])</pre>
```

```
regpath <- elnet(x, freenyy, alpha = c(0.5, 0.75))
plot(regpath)
plot(regpath, alpha = 0.75)
# Extract the coefficients at a certain penalization level
coef(regpath, lambda = regpath$lambda[[1]][[5]],
     alpha = 0.75)
# What penalization level leads to good prediction performance?
set.seed(123)
cv_results \le elnet_cv(x, freenyy, alpha = c(0.5, 0.75),
                       cv_repl = 10, cv_k = 4,
                       cv_measure = "tau")
plot(cv_results, se_mult = 1.5)
plot(cv_results, se_mult = 1.5, what = "coef.path")
# Extract the coefficients at the penalization level with
# smallest prediction error ...
summary(cv_results)
```

```
coef(cv_results)
# ... or at the penalization level with prediction error
# statistically indistinguishable from the minimum.
summary(cv_results, lambda = "1.5-se")
coef(cv_results, lambda = "1.5-se")
```

```
enpy
```

Deprecated

Description

[Deprecated]

Compute initial estimates for EN S-estimates using ENPY. Superseded by enpy_initial_estimates().

Usage

enpy(x, y, alpha, lambda, delta, cc, options, en_options)

Arguments

x	data matrix with predictors.
У	response vector.
alpha,lambda	EN penalty parameters (NOT adjusted for the number of observations in x).
delta	desired breakdown point of the resulting estimator.
сс	tuning constant for the S-estimator. Default is to chosen based on the breakdown point delta. Should never have to be changed.
options	ignored. Additional options for the initial estimator.
en_options	ignored. Additional options for the EN algorithm.

Value

coeff	A numeric matrix with one initial coefficient per column
objF	A vector of values of the objective function for the respective coefficient

Warning

Do not use this function in new code. It may be removed from future versions of the package.

See Also

Other deprecated functions: deprecated_en_options, initest_options(), mstep_options(),
pense_options(), pensem()

enpy_initial_estimates

ENPY Initial Estimates for EN S-Estimators

Description

Compute initial estimates for the EN S-estimator using the EN-PY procedure.

Usage

```
enpy_initial_estimates(
    x,
    y,
    alpha,
    lambda,
    bdp = 0.25,
    cc,
    intercept = TRUE,
    penalty_loadings,
    enpy_opts = enpy_options(),
    mscale_opts = mscale_algorithm_options(),
    eps = 1e-06,
    sparse = FALSE,
    ncores = 1L
)
```

Arguments

х	n by p matrix of numeric predictors.
У	vector of response values of length n.
alpha	elastic net penalty mixing parameter with $0 \le \alpha \le 1$. alpha = 1 is the LASSO penalty, and alpha = 0 the Ridge penalty. Can be a vector of several values, but alpha = 0 cannot be mixed with other values.

lambda	a vector of positive values of penalization levels.
bdp	desired breakdown point of the estimator, between 0.05 and 0.5. The actual breakdown point may be slightly larger/smaller to avoid instabilities of the S-loss.
сс	cutoff value for the bisquare rho function. By default, chosen to yield a consistent estimate for the Normal distribution.
intercept	include an intercept in the model.
penalty_loading	gs
	a vector of positive penalty loadings (a.k.a. weights) for different penalization of each coefficient. Only allowed for $alpha > 0$.
enpy_opts	options for the EN-PY algorithm, created with the enpy_options() function.
mscale_opts	options for the M-scale estimation. See <pre>mscale_algorithm_options()</pre> for de- tails.
eps	numerical tolerance.
sparse	use sparse coefficient vectors.
ncores	number of CPU cores to use in parallel. By default, only one CPU core is used. Not supported on all platforms, in which case a warning is given.

Details

If these manually computed initial estimates are intended as starting points for pense(), they are by default *shared* for all penalization levels. To restrict the use of the initial estimates to the penalty level they were computed for, use as_starting_point(..., specific = TRUE). See as_starting_point() for details.

References

Cohen Freue, G.V.; Kepplinger, D.; Salibián-Barrera, M.; Smucler, E. Robust elastic net estimators for variable selection and identification of proteomic biomarkers. *Ann. Appl. Stat.* **13** (2019), no. 4, 2065–2090 doi:10.1214/19AOAS1269

See Also

Other functions for initial estimates: prinsens(), starting_point()

enpy_options

Options for the ENPY Algorithm

Description

Additional control options for the elastic net Peña-Yohai procedure.

enpy_options

Usage

```
enpy_options(
  max_it = 10,
  keep_psc_proportion = 0.5,
  en_algorithm_opts,
  keep_residuals_measure = c("threshold", "proportion"),
  keep_residuals_proportion = 0.5,
  keep_residuals_threshold = 2,
  retain_best_factor = 2,
  retain_max = 500
)
```

Arguments

max_it	maximum number of EN-PY iterations.
keep_psc_propo	rtion
	how many observations should to keep based on the Principal Sensitivity Com-
	ponents.
en_algorithm_op	ots
	options for the LS-EN algorithm. See en_algorithm_options for details.
keep_residuals	_measure
	how to determine what observations to keep, based on their residuals. If proportion, a fixed number of observations is kept. If threshold, only observations with residuals below the threshold are kept.
keep_residuals	_proportion
	proportion of observations to kept based on their residuals.
keep_residuals	_threshold
	only observations with (standardized) residuals less than this threshold are kept.
retain_best_fac	ctor
	only keep candidates that are within this factor of the best candidate. If ≤ 1 , only keep candidates from the last iteration.
retain_max	maximum number of candidates, i.e., only the best retain_max candidates are retained.

Details

The EN-PY procedure for computing initial estimates iteratively cleans the data of observations with possibly outlying residual or high leverage. Least-squares elastic net (LS-EN) estimates are computed on the possibly clean subsets. At each iteration, the Principal Sensitivity Components are computed to remove observations with potentially high leverage. Among all the LS-EN estimates, the estimate with smallest M-scale of the residuals is selected. Observations with largest residual for the selected estimate are removed and the next iteration is started.

Value

options for the ENPY algorithm.

en_admm_options

Description

Use the ADMM Elastic Net Algorithm

Usage

```
en_admm_options(max_it = 1000, step_size, acceleration = 1)
```

Arguments

max_it	maximum number of iterations.
step_size	step size for the algorithm.
acceleration	acceleration factor for linearized ADMM.

Value

options for the ADMM EN algorithm.

See Also

Other EN algorithms: en_cd_options(), en_dal_options(), en_lars_options()

en_algorithm_options Control the Algorithm to Compute (Weighted) Least-Squares Elastic Net Estimates

Description

The package supports different algorithms to compute the EN estimate for weighted LS loss functions. Each algorithm has certain characteristics that make it useful for some problems. To select a specific algorithm and adjust the options, use any of the en_***_options functions.

Details

- en_lars_options(): Use the tuning-free LARS algorithm. This computes *exact* (up to numerical errors) solutions to the EN-LS problem. It is not iterative and therefore can not benefit from approximate solutions, but in turn guarantees that a solution will be found.
- en_cd_options(): Use an iterative coordinate descent algorithm which needs O(np) operations per iteration and converges sub-linearly.
- en_admm_options(): Use an iterative ADMM-type algorithm which needs O(np) operations per iteration and converges sub-linearly.
- en_dal_options(): Use the iterative Dual Augmented Lagrangian (DAL) method. DAL needs $O(n^3p^2)$ operations per iteration, but converges exponentially.

en_cd_options

Description

Use Coordinate Descent to Solve Elastic Net Problems

Usage

en_cd_options(max_it = 1000, reset_it = 8)

Arguments

max_it	maximum number of iterations.
reset_it	number of iterations after which the residuals are re-computed from scratch, to prevent numerical drifts from incremental updates.

See Also

Other EN algorithms: en_admm_options(), en_dal_options(), en_lars_options()

en_dal_options Use the DAL Elastic Net Algorithm

Description

Use the DAL Elastic Net Algorithm

Usage

```
en_dal_options(
  max_it = 100,
  max_inner_it = 100,
  eta_multiplier = 2,
  eta_start_conservative = 0.01,
  eta_start_aggressive = 1,
  lambda_relchange_aggressive = 0.25
)
```

Arguments

max_it	maximum number of (outer) iterations.
max_inner_it	maximum number of (inner) iterations in each outer iteration.
eta_multiplier	multiplier for the barrier parameter. In each iteration, the barrier must be more restrictive (i.e., the multiplier must be > 1).
eta_start_conse	rvative conservative initial barrier parameter. This is used if the previous penalty is undefined or too far away.
eta_start_aggre	ssive
	aggressive initial barrier parameter. This is used if the previous penalty is close.
lambda_relchang	e_aggressive
	how close must the lambda parameter from the previous penalty term be to use an aggressive initial barrier parameter (i.e., what constitutes "too far").

Value

options for the DAL EN algorithm.

See Also

Other EN algorithms: en_admm_options(), en_cd_options(), en_lars_options()

en_lars_options Use the LARS Elastic Net Algorithm

Description

Use the LARS Elastic Net Algorithm

Usage

en_lars_options()

See Also

Other EN algorithms: en_admm_options(), en_cd_options(), en_dal_options()

Description

[Deprecated]

Options for computing initial estimates via ENPY. Superseded by enpy_options().

Usage

```
initest_options(
   keep_solutions = 5,
   psc_method = c("exact", "rr"),
   maxit = 10,
   maxit_pense_refinement = 5,
   eps = 1e-06,
   psc_keep = 0.5,
   resid_keep_method = c("proportion", "threshold"),
   resid_keep_prop = 0.6,
   resid_keep_thresh = 2,
   mscale_eps = 1e-08,
   mscale_maxit = 200
)
```

Arguments

keep_solutions	how many initial estimates should be kept to perform full PENSE iterations?
psc_method	The method to use for computing the principal sensitivity components. See details for the possible choices.
<pre>maxit maxit_pense_ref</pre>	maximum number of refinement iterations. finement ignored. Maximum number of PENSE iterations to refine initial estimator.
eps	ignored. Numeric tolerance for convergence.
psc_keep	proportion of observations to keep based on the PSC scores.
resid_keep_meth	nod
	How to clean the data based on large residuals. If "proportion", observations with the smallest resid_keep_prop residuals will be retained. If "threshold", all observations with scaled residuals smaller than the threshold resid_keep_thresh will be retained.
resid_keep_prop	p,resid_keep_thresh
	proportion or threshold for observations to keep based on their residual.
<pre>mscale_eps, msca</pre>	ale_maxit
	ignored. Maximum number of iterations and numeric tolerance for the M-scale.

Warning

Do not use this function in new code. It may be removed from future versions of the package.

See Also

Other deprecated functions: deprecated_en_options, enpy(), mstep_options(), pense_options(), pensem()

mloc

Compute the M-estimate of Location

Description

Compute the M-estimate of location using an auxiliary estimate of the scale.

Usage

mloc(x, scale, rho, cc, opts = mscale_algorithm_options())

Arguments

x	numeric values. Missing values are verbosely ignored.
scale	scale of the x values. If omitted, uses the mad().
rho	the ρ function to use. See rho_function() for available functions.
сс	value of the tuning constant for the chosen ρ function. By default, chosen to achieve 95% efficiency under the Normal distribution.
opts	a list of options for the M-estimating algorithm, see mscale_algorithm_options() for details.

Value

a single numeric value, the M-estimate of location.

See Also

Other functions to compute robust estimates of location and scale: mlocscale(), mscale(), tau_size()

mlocscale

Description

Simultaneous estimation of the location and scale by means of M-estimates.

Usage

```
mlocscale(
    x,
    bdp = 0.25,
    scale_cc = consistency_const(bdp, "bisquare"),
    location_rho,
    location_cc,
    opts = mscale_algorithm_options()
)
```

Arguments

x	numeric values. Missing values are verbosely ignored.
bdp	desired breakdown point (between 0 and 0.5).
scale_cc	cutoff value for the bisquare ρ function for computing the scale estimate. By default, chosen to yield a consistent estimate for normally distributed values.
location_rho,l	ocation_cc ρ function and cutoff value for computing the location estimate. See rho_function() for a list of available ρ functions.
opts	a list of options for the M-estimating equation, see mscale_algorithm_options() for details.

Value

a vector with 2 elements, the M-estimate of location and the M-scale estimate.

See Also

Other functions to compute robust estimates of location and scale: mloc(), mscale(), tau_size()

mm_algorithm_options MM-Algorithm to Compute Penalized Elastic Net S- and M-Estimates

Description

Additional options for the MM algorithm to compute EN S- and M-estimates.

Usage

```
mm_algorithm_options(
    max_it = 500,
    tightening = c("adaptive", "exponential", "none"),
    tightening_steps = 2,
    en_algorithm_opts
)
```

Arguments

max_it	maximum number of iterations.
tightening	how to make inner iterations more precise as the algorithm approaches a local minimum.
tightening_step)S
	for <i>adaptive</i> tightening strategy, how often to tighten until the desired tolerance is attained.
en_algorithm_op	ots
	options for the inner LS-EN algorithm. See en_algorithm_options for details.

Value

options for the MM algorithm.

See Also

cd_algorithm_options for a direct optimization of the non-convex PENSE loss.

mscale

Compute the M-Scale of Centered Values

Description

Compute the M-scale without centering the values.

Usage

```
mscale(
    x,
    bdp = 0.25,
    cc = consistency_const(bdp, "bisquare"),
    opts = mscale_algorithm_options(),
    delta = deprecated(),
    rho = deprecated(),
    eps = deprecated(),
    maxit = deprecated()
)
```

Arguments

х	numeric values. Missing values are verbosely ignored.
bdp	desired breakdown point (between 0 and 0.5).
сс	cutoff value for the bisquare rho function. By default, chosen to yield a consistent estimate for the Normal distribution.
opts	a list of options for the M-scale estimation algorithm, see $mscale_algorithm_options()$ for details.
delta	deprecated. Use bpd instead.
rho,eps,maxit	deprecated. Instead set control options for the algorithm with the opts arguments.

Value

the M-estimate of scale.

See Also

Other functions to compute robust estimates of location and scale: mloc(), mlocscale(), tau_size()

mscale_algorithm_options

Options for the M-scale Estimation Algorithm

Description

Options for the M-scale Estimation Algorithm

Usage

```
mscale_algorithm_options(max_it = 200, eps = 1e-08)
```

Arguments

max_it	maximum number of iterations.
eps	numerical tolerance to check for convergence.

Value

options for the M-scale estimation algorithm.

Description

[Deprecated]

Additional options for computing penalized EN MM-estimates. Superseded by mm_algorithm_options() and options supplied directly to pensem_cv().

Usage

```
mstep_options(
  cc = 3.44,
  maxit = 1000,
  eps = 1e-06,
  adjust_bdp = FALSE,
  verbosity = 0,
  en_correction = TRUE
)
```

Arguments

сс	ignored. Tuning constant for the M-estimator.
maxit	maximum number of iterations allowed.
eps	ignored. Numeric tolerance for convergence.
adjust_bdp	ignored. Should the breakdown point be adjusted based on the effective degrees of freedom?
verbosity	ignored. Verbosity of the algorithm.
en_correction	ignored. Should the corrected EN estimator be used to choose the optimal lambda with CV. If TRUE, as by default, the estimator is "bias corrected".

Warning

Do not use this function in new code. It may be removed from future versions of the package.

See Also

Other deprecated functions: deprecated_en_options, enpy(), initest_options(), pense_options(), pensem()

pense

Description

Compute elastic net S-estimates (PENSE estimates) along a grid of penalization levels with optional penalty loadings for adaptive elastic net.

Usage

```
pense(
  х,
  у,
  alpha,
  nlambda = 50,
  nlambda_enpy = 10,
  lambda,
  lambda_min_ratio,
  enpy_lambda,
  penalty_loadings,
  intercept = TRUE,
  bdp = 0.25,
  cc,
  add_zero_based = TRUE,
  enpy_specific = FALSE,
  other_starts,
  carry_forward = TRUE,
  eps = 1e-06,
  explore_solutions = 10,
  explore_tol = 0.1,
  explore_it = 5,
 max_solutions = 1,
  comparison_tol = sqrt(eps),
  sparse = FALSE,
  ncores = 1,
  standardize = TRUE,
  algorithm_opts = mm_algorithm_options(),
 mscale_opts = mscale_algorithm_options(),
  enpy_opts = enpy_options(),
  cv_k = deprecated(),
  cv_objective = deprecated(),
  . . .
)
```

/

Arguments

Х

n by p matrix of numeric predictors.

У	vector of response values of length n. For binary classification, y should be a factor with 2 levels.
alpha	elastic net penalty mixing parameter with $0 \le \alpha \le 1$. alpha = 1 is the LASSO penalty, and alpha = 0 the Ridge penalty. Can be a vector of several values, but alpha = 0 cannot be mixed with other values.
nlambda	number of penalization levels.
nlambda_enpy	number of penalization levels where the EN-PY initial estimate is computed.
lambda	optional user-supplied sequence of penalization levels. If given and not NULL, nlambda and lambda_min_ratio are ignored.
lambda_min_rati	io
	Smallest value of the penalization level as a fraction of the largest level (i.e., the smallest value for which all coefficients are zero). The default depends on the sample size relative to the number of variables and alpha. If more observations than variables are available, the default is $1e-3 \times alpha$, otherwise $1e-2 \times alpha$.
enpy_lambda	optional user-supplied sequence of penalization levels at which EN-PY initial estimates are computed. If given and not NULL, nlambda_enpy is ignored.
penalty_loading	-
	a vector of positive penalty loadings (a.k.a. weights) for different penalization of each coefficient. Only allowed for $alpha > 0$.
intercept	include an intercept in the model.
bdp	desired breakdown point of the estimator, between 0.05 and 0.5. The actual breakdown point may be slightly larger/smaller to avoid instabilities of the S-loss.
сс	tuning constant for the S-estimator. Default is chosen based on the breakdown point bdp. This affects the estimated coefficients only if standardize=TRUE. Otherwise only the estimated scale of the residuals would be affected.
add_zero_based	also consider the 0-based regularization path. See details for a description.
<pre>enpy_specific</pre>	use the EN-PY initial estimates only at the penalization level they are computed for. See details for a description.
other_starts	a list of other staring points, created by starting_point(). If the output of enpy_initial_estimates() is given, the starting points will be <i>shared</i> among all penalization levels. Note that if a the starting point is <i>specific</i> to a penalization level, this penalization level is added to the grid of penalization levels (either the manually specified grid in lambda or the automatically generated grid of size nlambda). If standardize = TRUE, the starting points are also scaled.
carry_forward	carry the best solutions forward to the next penalty level.
eps explore_solution	numerical tolerance.
number of solutions to compute up to the desired precision eps.	
explore_tol, explore_it	
	numerical tolerance and maximum number of iterations for exploring possible solutions. The tolerance should be (much) looser than eps to be useful, and the number of iterations should also be much smaller than the maximum number of iterations given via algorithm_opts.

pense

<pre>max_solutions</pre>	only retain up to max_solutions unique solutions per penalization level.
comparison_tol	numeric tolerance to determine if two solutions are equal. The comparison is first done on the absolute difference in the value of the objective function at the solution If this is less than comparison_tol, two solutions are deemed equal if the squared difference of the intercepts is less than comparison_tol and the squared L_2 norm of the difference vector is less than comparison_tol.
sparse	use sparse coefficient vectors.
ncores	number of CPU cores to use in parallel. By default, only one CPU core is used. Not supported on all platforms, in which case a warning is given.
standardize	logical flag to standardize the x variables prior to fitting the PENSE estimates. Coefficients are always returned on the original scale. This can fail for variables with a large proportion of a single value (e.g., zero-inflated data). In this case, either compute with standardize = FALSE or standardize the data manually.
algorithm_opts	options for the MM algorithm to compute the estimates. See mm_algorithm_options() for details.
mscale_opts	options for the M-scale estimation. See <pre>mscale_algorithm_options()</pre> for de- tails.
enpy_opts	options for the ENPY initial estimates, created with the enpy_options() func- tion. See enpy_initial_estimates() for details.
cv_k, cv_objective	
	deprecated and ignored. See pense_cv() for estimating prediction performance via cross-validation.
	ignored. See the section on deprecated parameters below.

Value

a list-like object with the following items

alpha the sequence of alpha parameters.

lambda a list of sequences of penalization levels, one per alpha parameter.

estimates a list of estimates. Each estimate contains the following information:

intercept intercept estimate.

beta beta (slope) estimate.

lambda penalization level at which the estimate is computed.

alpha *alpha* hyper-parameter at which the estimate is computed.

bdp chosen breakdown-point.

objf_value value of the objective function at the solution.

statuscode if > 0 the algorithm experienced issues when computing the estimate.

status optional status message from the algorithm.

bdp the actual breakdown point used.

call the original call.

Strategies for Using Starting Points

The function supports several different strategies to compute, and use the provided starting points for optimizing the PENSE objective function.

Starting points are computed internally but can also be supplied via other_starts. By default, starting points are computed internally by the EN-PY procedure for penalization levels supplied in enpy_lambda (or the automatically generated grid of length nlambda_enpy). By default, starting points computed by the EN-PY procedure are *shared* for all penalization levels in lambda (or the automatically generated grid of length nlambda). If the starting points should be *specific* to the penalization level the starting points' penalization level, set the enpy_specific argument to TRUE.

In addition to EN-PY initial estimates, the algorithm can also use the "0-based" strategy if add_zero_based = TRUE (by default). Here, the 0-vector is used to start the optimization at the largest penalization level in lambda. At subsequent penalization levels, the solution at the previous penalization level is also used as starting point.

At every penalization level, all starting points are explored using the loose numerical tolerance explore_tol. Only the best explore_solutions are computed to the stringent numerical tolerance eps. Finally, only the best max_solutions are retained and carried forward as starting points for the subsequent penalization level.

Deprecated Arguments

Starting with version 2.0.0, cross-validation is performed by separate function pense_cv(). Arguments related cross-validation cause an error when supplied to pense(). Furthermore, the following arguments are deprecated as of version 2.0.0: initial, warm_reset, cl, options, init_options, en_options. If pense() is called with any of these arguments, warnings detail how to replace them.

See Also

pense_cv() for selecting hyper-parameters via cross-validation.

coef.pense_fit() for extracting coefficient estimates.

plot.pense_fit() for plotting the regularization path.

Other functions to compute robust estimates: regmest()

Examples

```
# Compute the PENSE regularization path for Freeny's revenue data
# (see ?freeny)
data(freeny)
x <- as.matrix(freeny[ , 2:5])
regpath <- pense(x, freeny$y, alpha = 0.5)
plot(regpath)
# Extract the coefficients at a certain penalization level
coef(regpath, lambda = regpath$lambda[[1]][[40]])
# What penalization level leads to good prediction performance?
set.seed(123)
```

pensem

pensem

Deprecated Alias of pensem_cv

Description

pensem() is a deprecated alias for pensem_cv().

Usage

pensem(x, ...)

Arguments

Х	either a numeric matrix of predictor values, or a cross-validated PENSE fit from
	pense_cv().
	ignored. See the section on deprecated parameters below.

See Also

Other deprecated functions: deprecated_en_options, enpy(), initest_options(), mstep_options(),
pense_options()

pensem_cv

Compute Penalized Elastic Net M-Estimates from PENSE

Description

This is a convenience wrapper around pense_cv() and regmest_cv(), for the common use-case of computing a highly-robust S-estimate followed by a more efficient M-estimate using the scale of the residuals from the S-estimate.

Usage

```
pensem_cv(x, ...)
## Default S3 method:
pensem_cv(
  х,
 у,
  alpha = 0.5,
  nlambda = 50,
  lambda_min_ratio,
  lambda_m,
  lambda_s,
  standardize = TRUE,
  penalty_loadings,
  intercept = TRUE,
  bdp = 0.25,
  ncores = 1,
  sparse = FALSE,
  eps = 1e-06,
  cc = 4.7,
  cv_k = 5,
  cv_repl = 1,
  cl = NULL,
  cv_metric = c("tau_size", "mape", "rmspe"),
  add_zero_based = TRUE,
  explore_solutions = 10,
  explore_tol = 0.1,
  explore_it = 5,
  max_solutions = 10,
  fit_all = TRUE,
  comparison_tol = sqrt(eps),
  algorithm_opts = mm_algorithm_options(),
 mscale_opts = mscale_algorithm_options(),
  nlambda_enpy = 10,
  enpy_opts = enpy_options(),
  . . .
)
## S3 method for class 'pense_cvfit'
pensem_cv(
  х,
  scale,
  alpha,
  nlambda = 50,
  lambda_min_ratio,
  lambda_m,
  standardize = TRUE,
  penalty_loadings,
```

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pensem_cv

```
intercept = TRUE,
bdp = 0.25,
ncores = 1,
sparse = FALSE,
eps = 1e-06,
cc = 4.7,
cv_k = 5,
cv_repl = 1,
cl = NULL,
cv_metric = c("tau_size", "mape", "rmspe"),
add_zero_based = TRUE,
explore_solutions = 10,
explore_tol = 0.1,
explore_it = 5,
max_solutions = 10,
fit_all = TRUE,
comparison_tol = sqrt(eps),
algorithm_opts = mm_algorithm_options(),
mscale_opts = mscale_algorithm_options(),
x_train,
y_train,
• • •
```

Arguments

)

x	either a numeric matrix of predictor values, or a cross-validated PENSE fit from pense_cv().
	ignored. See the section on deprecated parameters below.
У	vector of response values of length n. For binary classification, y should be a factor with 2 levels.
alpha	elastic net penalty mixing parameter with $0 \le \alpha \le 1$. alpha = 1 is the LASSO penalty, and alpha = 0 the Ridge penalty. Can be a vector of several values, but alpha = 0 cannot be mixed with other values.
nlambda	number of penalization levels.
lambda_min_rati	0
	Smallest value of the penalization level as a fraction of the largest level (i.e., the smallest value for which all coefficients are zero). The default depends on the sample size relative to the number of variables and alpha. If more observations than variables are available, the default is $1e-3 \times alpha$, otherwise $1e-2 \times alpha$.
lambda_m,lambda_s	
	optional user-supplied sequence of penalization levels for the S- and M-estimates. If given and not NULL, nlambda and lambda_min_ratio are ignored for the respective estimate (S and/or M).
standardize	logical flag to standardize the x variables prior to fitting the PENSE estimates. Coefficients are always returned on the original scale. This can fail for variables

	with a large proportion of a single value (e.g., zero-inflated data). In this case,
	either compute with standardize = FALSE or standardize the data manually.
penalty_loading	-
	a vector of positive penalty loadings (a.k.a. weights) for different penalization of each coefficient. Only allowed for $alpha > 0$.
intercept	include an intercept in the model.
bdp	desired breakdown point of the estimator, between 0.05 and 0.5. The actual breakdown point may be slightly larger/smaller to avoid instabilities of the S-loss.
ncores	number of CPU cores to use in parallel. By default, only one CPU core is used. Not supported on all platforms, in which case a warning is given.
sparse	use sparse coefficient vectors.
eps	numerical tolerance.
сс	cutoff constant for Tukey's bisquare ρ function in the M-estimation objective function.
cv_k	number of folds per cross-validation.
cv_repl	number of cross-validation replications.
cl	a parallel cluster. Can only be used in combination with ncores = 1.
cv_metric	either a string specifying the performance metric to use, or a function to eval- uate prediction errors in a single CV replication. If a function, the number of arguments define the data the function receives. If the function takes a single argument, it is called with a single numeric vector of prediction errors. If the function takes two or more arguments, it is called with the predicted values as first argument and the true values as second argument. The function must al- ways return a single numeric value quantifying the prediction performance. The order of the given values corresponds to the order in the input data.
	also consider the 0-based regularization path. See details for a description.
explore_solution	
explore_tol, exp	number of solutions to compute up to the desired precision eps.
	numerical tolerance and maximum number of iterations for exploring possible solutions. The tolerance should be (much) looser than eps to be useful, and the number of iterations should also be much smaller than the maximum number of iterations given via algorithm_opts.
<pre>max_solutions</pre>	only retain up to max_solutions unique solutions per penalization level.
fit_all	If TRUE, fit the model for all penalization levels. Can also be any combination of "min" and "{x}-se", in which case only models at the penalization level with smallest average CV accuracy, or within {x} standard errors, respectively. Setting fit_all to FALSE is equivalent to "min". Applies to all alpha value.
comparison_tol	numeric tolerance to determine if two solutions are equal. The comparison is first done on the absolute difference in the value of the objective function at the solution If this is less than comparison_tol, two solutions are deemed equal if the squared difference of the intercepts is less than comparison_tol and the squared L_2 norm of the difference vector is less than comparison_tol.

pense_cv

algorithm_opts	options for the MM algorithm to compute the estimates. See mm_algorithm_options() for details.
mscale_opts	options for the M-scale estimation. See <pre>mscale_algorithm_options()</pre> for de- tails.
nlambda_enpy	number of penalization levels where the EN-PY initial estimate is computed.
enpy_opts	options for the ENPY initial estimates, created with the enpy_options() func- tion. See enpy_initial_estimates() for details.
scale	initial scale estimate to use in the M-estimation. By default the S-scale from the PENSE fit is used.
x_train, y_train	
	override arguments x and y as provided in the call to $pense_cv()$. This is useful if the arguments in the $pense_cv()$ call are not available in the current environment.

Details

The built-in CV metrics are

"tau_size" τ -size of the prediction error, computed by tau_size() (default).

"mape" Median absolute prediction error.

"rmspe" Root mean squared prediction error.

"auroc" Area under the receiver operator characteristic curve (actually 1 - AUROC). Only sensible for binary responses.

Value

an object of cross-validated regularized M-estimates as returned from regmest_cv().

See Also

pense_cv() to compute the starting S-estimate.

Other functions to compute robust estimates with CV: pense_cv(), regmest_cv()

pense_cv

Cross-validation for (Adaptive) PENSE Estimates

Description

Perform (repeated) K-fold cross-validation for pense().

adapense_cv() is a convenience wrapper to compute adaptive PENSE estimates.

Usage

```
pense_cv(
    x,
    y,
    standardize = TRUE,
    lambda,
    cv_k,
    cv_repl = 1,
    cv_metric = c("tau_size", "mape", "rmspe", "auroc"),
    fit_all = TRUE,
    fold_starts = c("full", "enpy", "both"),
    cl = NULL,
    ...
)
```

adapense_cv(x, y, alpha, alpha_preliminary = 0, exponent = 1, ...)

Arguments

x	n by p matrix of numeric predictors.
У	vector of response values of length n. For binary classification, y should be a factor with 2 levels.
standardize	whether to standardize the x variables prior to fitting the PENSE estimates. Can also be set to "cv_only", in which case the input data is not standardized, but the training data in the CV folds is scaled to match the scaling of the input data. Coefficients are always returned on the original scale. This can fail for variables with a large proportion of a single value (e.g., zero-inflated data). In this case, either compute with standardize = FALSE or standardize the data manually.
lambda	optional user-supplied sequence of penalization levels. If given and not NULL, nlambda and lambda_min_ratio are ignored.
cv_k	number of folds per cross-validation.
cv_repl	number of cross-validation replications.
cv_metric	either a string specifying the performance metric to use, or a function to eval- uate prediction errors in a single CV replication. If a function, the number of arguments define the data the function receives. If the function takes a single argument, it is called with a single numeric vector of prediction errors. If the function takes two or more arguments, it is called with the predicted values as first argument and the true values as second argument. The function must al- ways return a single numeric value quantifying the prediction performance. The order of the given values corresponds to the order in the input data.
fit_all	If TRUE, fit the model for all penalization levels. Can also be any combination of "min" and "{x}-se", in which case only models at the penalization level with smallest average CV accuracy, or within {x} standard errors, respectively. Setting fit_all to FALSE is equivalent to "min". Applies to all alpha value.
fold_starts	how to determine starting values in the cross-validation folds. If "full" (de- fault), use the best solution from the fit to the full data as starting value. This

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implies fit_all=TRUE. If "enpy" compute separate ENPY initial estimates in each fold. The option "both" uses both. These starts are in addition to the starts provided in other_starts.

a parallel cluster. Can only be used in combination with ncores = 1.

Arguments passed on to pense

nlambda number of penalization levels.

- lambda_min_ratio Smallest value of the penalization level as a fraction of the largest level (i.e., the smallest value for which all coefficients are zero). The default depends on the sample size relative to the number of variables and alpha. If more observations than variables are available, the default is 1e-3 * alpha, otherwise 1e-2 * alpha.
- nlambda_enpy number of penalization levels where the EN-PY initial estimate is computed.
- penalty_loadings a vector of positive penalty loadings (a.k.a. weights) for different penalization of each coefficient. Only allowed for alpha > 0.
- enpy_lambda optional user-supplied sequence of penalization levels at which EN-PY initial estimates are computed. If given and not NULL, nlambda_enpy is ignored.
- other_starts a list of other staring points, created by starting_point(). If the output of enpy_initial_estimates() is given, the starting points will be *shared* among all penalization levels. Note that if a the starting point is *specific* to a penalization level, this penalization level is added to the grid of penalization levels (either the manually specified grid in lambda or the automatically generated grid of size nlambda). If standardize = TRUE, the starting points are also scaled.
- intercept include an intercept in the model.
- bdp desired breakdown point of the estimator, between 0.05 and 0.5. The actual breakdown point may be slightly larger/smaller to avoid instabilities of the S-loss.
- cc tuning constant for the S-estimator. Default is chosen based on the breakdown point bdp. This affects the estimated coefficients only if standardize=TRUE. Otherwise only the estimated scale of the residuals would be affected.
- eps numerical tolerance.
- explore_solutions number of solutions to compute up to the desired precision eps.
- explore_tol,explore_it numerical tolerance and maximum number of iterations for exploring possible solutions. The tolerance should be (much) looser than eps to be useful, and the number of iterations should also be much smaller than the maximum number of iterations given via algorithm_opts.
- max_solutions only retain up to max_solutions unique solutions per penalization level.
- comparison_tol numeric tolerance to determine if two solutions are equal. The comparison is first done on the absolute difference in the value of the objective function at the solution If this is less than comparison_tol, two solutions are deemed equal if the squared difference of the intercepts is less than comparison_tol and the squared L_2 norm of the difference vector is less than comparison_tol.

cl ...

	add_zero_based also consider the 0-based regularization path. See details for a description.
	enpy_specific use the EN-PY initial estimates only at the penalization level they are computed for. See details for a description.
	carry_forward carry the best solutions forward to the next penalty level.
	sparse use sparse coefficient vectors.
	ncores number of CPU cores to use in parallel. By default, only one CPU core is used. Not supported on all platforms, in which case a warning is given.
	algorithm_opts options for the MM algorithm to compute the estimates. See mm_algorithm_options() for details.
	<pre>mscale_opts options for the M-scale estimation. See mscale_algorithm_options() for details.</pre>
	<pre>enpy_opts options for the ENPY initial estimates, created with the enpy_options() function. See enpy_initial_estimates() for details.</pre>
	<pre>cv_k,cv_objective deprecated and ignored. See pense_cv() for estimating prediction performance via cross-validation.</pre>
alpha	elastic net penalty mixing parameter with $0 \le \alpha \le 1$. alpha = 1 is the LASSO penalty, and alpha = 0 the Ridge penalty. Can be a vector of several values, but alpha = 0 cannot be mixed with other values.
alpha_prelimina	ary
	alpha parameter for the preliminary estimate.
exponent	the exponent for computing the penalty loadings based on the preliminary esti- mate.

Details

The built-in CV metrics are

- "tau_size" τ -size of the prediction error, computed by tau_size() (default).
- "mape" Median absolute prediction error.
- "rmspe" Root mean squared prediction error.
- "auroc" Area under the receiver operator characteristic curve (actually 1 AUROC). Only sensible for binary responses.

adapense_cv() is a convenience wrapper which performs 3 steps:

- 1. compute preliminary estimates via pense_cv(..., alpha = alpha_preliminary),
- 2. computes the penalty loadings from the estimate beta with best prediction performance by adapense_loadings = 1 / abs(beta)^exponent, and
- 3. compute the adaptive PENSE estimates via pense_cv(..., penalty_loadings = adapense_loadings).

Value

a list-like object with the same components as returned by pense(), plus the following:

cvres data frame of average cross-validated performance.

pense_cv

a list-like object as returned by pense_cv() plus the following

preliminary the CV results for the preliminary estimate.

exponent exponent used to compute the penalty loadings.

penalty_loadings penalty loadings used for the adaptive PENSE estimate.

See Also

pense() for computing regularized S-estimates without cross-validation.

coef.pense_cvfit() for extracting coefficient estimates.

plot.pense_cvfit() for plotting the CV performance or the regularization path.

Other functions to compute robust estimates with CV: pensem_cv(), regmest_cv()

Other functions to compute robust estimates with CV: pensem_cv(), regmest_cv()

Examples

```
# Compute the adaptive PENSE regularization path for Freeny's
# revenue data (see ?freeny)
data(freeny)
x <- as.matrix(freeny[ , 2:5])</pre>
## Either use the convenience function directly ...
set.seed(123)
ada_convenience <- adapense_cv(x, freenyy, alpha = 0.5,
                                cv_repl = 2, cv_k = 4)
## ... or compute the steps manually:
# Step 1: Compute preliminary estimates with CV
set.seed(123)
preliminary_estimate <- pense_cv(x, freeny$y, alpha = 0,</pre>
                                  cv_repl = 2, cv_k = 4)
plot(preliminary_estimate, se_mult = 1)
# Step 2: Use the coefficients with best prediction performance
# to define the penalty loadings:
prelim_coefs <- coef(preliminary_estimate, lambda = 'min')</pre>
pen_loadings <- 1 / abs(prelim_coefs[-1])</pre>
# Step 3: Compute the adaptive PENSE estimates and estimate
# their prediction performance.
set.seed(123)
ada_manual <- pense_cv(x, freeny$y, alpha = 0.5,</pre>
                        cv_repl = 2, cv_k = 4,
                        penalty_loadings = pen_loadings)
# Visualize the prediction performance and coefficient path of
# the adaptive PENSE estimates (manual vs. automatic)
def.par <- par(no.readonly = TRUE)</pre>
layout(matrix(1:4, ncol = 2, byrow = TRUE))
plot(ada_convenience$preliminary)
```

```
plot(preliminary_estimate)
plot(ada_convenience)
plot(ada_manual)
par(def.par)
```

pense_options Deprecated

Description

[Deprecated]

Additional options for computing penalized EN S-estimates. Superseded by mm_algorithm_options() and options supplied directly to pense().

Usage

```
pense_options(
    delta = 0.25,
    maxit = 1000,
    eps = 1e-06,
    mscale_eps = 1e-08,
    mscale_maxit = 200,
    verbosity = 0,
    cc = NULL,
    en_correction = TRUE
)
```

Arguments

delta	desired breakdown point of the resulting estimator.
maxit	maximum number of iterations allowed.
eps	numeric tolerance for convergence.
<pre>mscale_eps, msca</pre>	le_maxit
	maximum number of iterations and numeric tolerance for the M-scale.
verbosity	ignored. Verbosity of the algorithm.
сс	ignored. Tuning constant for the S-estimator. Default is to chosen based on the breakdown point delta. Should never have to be changed.
en_correction	ignored. Should the corrected EN estimator be used to choose the optimal lambda with CV. If TRUE, as by default, the estimator is "bias corrected".

Warning

Do not use this function in new code. It may be removed from future versions of the package.

See Also

Other deprecated functions: deprecated_en_options, enpy(), initest_options(), mstep_options(),
pensem()

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plot.pense_cvfit Plot Method for Penalized Estimates With Cross-Validation

Description

Plot the cross-validation performance or the coefficient path for fitted penalized elastic net S- or LS-estimates of regression.

Usage

```
## S3 method for class 'pense_cvfit'
plot(x, what = c("cv", "coef.path"), alpha = NULL, se_mult = 1, ...)
```

Arguments

х	fitted estimates with cross-validation information.
what	plot either the CV performance or the coefficient path.
alpha	If what = "cv", only CV performance for fits with matching alpha are plot- ted. In case alpha is missing or NULL, all fits in x are plotted. If what = "coef.path", plot the coefficient path for the fit with the given hyper-parameter value or, in case alpha is missing, for the first value in x\$alpha.
se_mult	if plotting CV performance, multiplier of the estimated SE.
	currently ignored.

See Also

Other functions for plotting and printing: plot.pense_fit(), prediction_performance(), summary.pense_cvfit()

Examples

```
# smallest prediction error ...
coef(cv_results)
# ... or at the penalization level with prediction error
# statistically indistinguishable from the minimum.
coef(cv_results, lambda = '1-se')
```

plot.pense_fit Plot Method for Penalized Estimates

Description

Plot the coefficient path for fitted penalized elastic net S- or LS-estimates of regression.

Usage

S3 method for class 'pense_fit'
plot(x, alpha, ...)

Arguments

х	fitted estimates.	
alpha	Plot the coefficient path for the fit with the given hyper-parameter value. missing of NULL, the first value in x\$alpha is used.	If
	currently ignored.	

See Also

Other functions for plotting and printing: plot.pense_cvfit(), prediction_performance(), summary.pense_cvfit()

Examples

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predict.pense_cvfit

```
# Extract the coefficients at the penalization level with
# smallest prediction error ...
coef(cv_results)
# ... or at the penalization level with prediction error
# statistically indistinguishable from the minimum.
coef(cv_results, lambda = '1-se')
```

predict.pense_cvfit Predict Method for PENSE Fits

Description

Predict response values using a PENSE (or LS-EN) regularization path with hyper-parameters chosen by cross-validation.

Usage

```
## S3 method for class 'pense_cvfit'
predict(
    object,
    newdata,
    alpha = NULL,
    lambda = "min",
    se_mult = 1,
    exact = deprecated(),
    correction = deprecated(),
    ...
)
```

Arguments

object	PENSE with cross-validated hyper-parameters to extract coefficients from.
newdata	an optional matrix of new predictor values. If missing, the fitted values are computed.
alpha	Either a single number or NULL (default). If given, only fits with the given alpha value are considered. If lambda is a numeric value and object was fit with multiple <i>alpha</i> values and no value is provided, the first value in object\$alpha is used with a warning.
lambda	either a string specifying which penalty level to use ("min", "se", "{m}-se") or a single numeric value of the penalty parameter. See details.
se_mult	If lambda = "se", the multiple of standard errors to tolerate.
exact	deprecated. Always gives a warning if lambda is not part of the fitted sequence and coefficients are interpolated.
correction	defunct.
	currently not used.

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Value

a numeric vector of residuals for the given penalization level.

Hyper-parameters

If lambda = "{m}-se" and object contains fitted estimates for every penalization level in the sequence, use the fit the most parsimonious model with prediction performance statistically indistinguishable from the best model. This is determined to be the model with prediction performance within $m \star cv_se$ from the best model. If lambda = "se", the multiplier *m* is taken from se_mult.

By default all *alpha* hyper-parameters available in the fitted object are considered. This can be overridden by supplying one or multiple values in parameter alpha. For example, if lambda = "1-se" and alpha contains two values, the "1-SE" rule is applied individually for each alpha value, and the fit with the better prediction error is considered.

In case lambda is a number and object was fit for several *alpha* hyper-parameters, alpha must also be given, or the first value in object\$alpha is used with a warning.

See Also

Other functions for extracting components: coef.pense_cvfit(), coef.pense_fit(), predict.pense_fit(), residuals.pense_cvfit(), residuals.pense_fit()

Examples

```
# Compute the LS-EN regularization path for Freeny's revenue data
# (see ?freeny)
data(freeny)
x <- as.matrix(freeny[ , 2:5])</pre>
regpath <- elnet(x, freeny$y, alpha = 0.75)</pre>
# Predict the response using a specific penalization level
predict(regpath, newdata = freeny[1:5, 2:5],
        lambda = regpath$lambda[[1]][[10]])
# Extract the residuals at a certain penalization level
residuals(regpath, lambda = regpath$lambda[[1]][[5]])
# Select penalization level via cross-validation
set.seed(123)
cv_results <- elnet_cv(x, freeny$y, alpha = 0.5,</pre>
                       cv_repl = 10, cv_k = 4)
# Predict the response using the "best" penalization level
predict(cv_results, newdata = freeny[1:5, 2:5])
# Extract the residuals at the "best" penalization level
residuals(cv_results)
# Extract the residuals at a more parsimonious penalization level
residuals(cv_results, lambda = "1.5-se")
```

Description

Predict response values using a PENSE (or LS-EN) regularization path fitted by pense(), regmest() or elnet().

Usage

```
## S3 method for class 'pense_fit'
predict(
    object,
    newdata,
    alpha = NULL,
    lambda,
    exact = deprecated(),
    correction = deprecated(),
    ...
)
```

Arguments

object	PENSE regularization path to extract residuals from.
newdata	an optional matrix of new predictor values. If missing, the fitted values are computed.
alpha	Either a single number or NULL (default). If given, only fits with the given alpha value are considered. If object was fit with multiple alpha values, and no value is provided, the first value in object\$alpha is used with a warning.
lambda	a single number for the penalty level.
exact	defunct Always gives a warning if lambda is not part of the fitted sequence and coefficients need to be interpolated.
correction	defunct.
	currently not used.

Value

a numeric vector of residuals for the given penalization level.

See Also

Other functions for extracting components: coef.pense_cvfit(), coef.pense_fit(), predict.pense_cvfit(), residuals.pense_cvfit(), residuals.pense_fit()

Examples

```
# Compute the LS-EN regularization path for Freeny's revenue data
# (see ?freeny)
data(freeny)
x <- as.matrix(freeny[ , 2:5])</pre>
regpath <- elnet(x, freeny$y, alpha = 0.75)</pre>
# Predict the response using a specific penalization level
predict(regpath, newdata = freeny[1:5, 2:5],
        lambda = regpath$lambda[[1]][[10]])
# Extract the residuals at a certain penalization level
residuals(regpath, lambda = regpath$lambda[[1]][[5]])
# Select penalization level via cross-validation
set.seed(123)
cv_results <- elnet_cv(x, freeny$y, alpha = 0.5,</pre>
                       cv_repl = 10, cv_k = 4)
# Predict the response using the "best" penalization level
predict(cv_results, newdata = freeny[1:5, 2:5])
# Extract the residuals at the "best" penalization level
residuals(cv_results)
# Extract the residuals at a more parsimonious penalization level
residuals(cv_results, lambda = "1.5-se")
```

prediction_performance

```
Prediction Performance of Adaptive PENSE Fits
```

Description

Extract the prediction performance of one or more (adaptive) PENSE fits.

Usage

```
prediction_performance(..., alpha = NULL, lambda = "min", se_mult = 1)
```

```
## S3 method for class 'pense_pred_perf'
print(x, ...)
```

Arguments

	one or more (adaptive) PENSE fits with cross-validation information.
alpha	Either a numeric vector or NULL (default). If given, only fits with the given alpha value are considered. If lambda is a numeric value and object was fit
	with multiple alpha values, the parameter alpha must not be missing.

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prinsens

lambda	either a string specifying which penalty level to use ("min", "se", "{x}-se") or a single numeric value of the penalty parameter. See details.
se_mult	If lambda = "se", the multiple of standard errors to tolerate.
x	an object with information on prediction performance created with prediction_performance().

Details

If lambda = "se" and the cross-validation was performed with multiple replications, use the penalty level whit prediction performance within se_mult of the best prediction performance.

Value

a data frame with details about the prediction performance of the given PENSE fits. The data frame has a custom print method summarizing the prediction performances.

See Also

summary.pense_cvfit() for a summary of the fitted model.

Other functions for plotting and printing: plot.pense_cvfit(), plot.pense_fit(), summary.pense_cvfit()

prinsens

Principal Sensitivity Components

Description

Compute Principal Sensitivity Components for Elastic Net Regression

Usage

```
prinsens(
    x,
    y,
    alpha,
    lambda,
    intercept = TRUE,
    penalty_loadings,
    en_algorithm_opts,
    eps = 1e-06,
    sparse = FALSE,
    ncores = 1L,
    method = deprecated()
)
```

Arguments

х	n by p matrix of numeric predictors.	
У	vector of response values of length n.	
alpha	elastic net penalty mixing parameter with $0 \le \alpha \le 1$. alpha = 1 is the LASSO penalty, and alpha = 0 the Ridge penalty. Can be a vector of several values, but alpha = 0 cannot be mixed with other values.	
lambda	optional user-supplied sequence of penalization levels. If given and not NULL, nlambda and lambda_min_ratio are ignored.	
intercept	include an intercept in the model.	
penalty_loadin	gs	
	a vector of positive penalty loadings (a.k.a. weights) for different penalization of each coefficient. Only allowed for $alpha > 0$.	
en_algorithm_opts		
	options for the LS-EN algorithm. See en_algorithm_options for details.	
eps	numerical tolerance.	
sparse	use sparse coefficient vectors.	
ncores	number of CPU cores to use in parallel. By default, only one CPU core is used. Not supported on all platforms, in which case a warning is given.	
method	defunct. PSCs are always computed for EN estimates. For the PY procedure for unpenalized estimation use package pyinit.	

Value

a list of principal sensitivity components, one per element in lambda. Each PSC is itself a list with items lambda, alpha, and pscs.

References

Cohen Freue, G.V.; Kepplinger, D.; Salibián-Barrera, M.; Smucler, E. Robust elastic net estimators for variable selection and identification of proteomic biomarkers. *Ann. Appl. Stat.* **13** (2019), no. 4, 2065–2090 doi:10.1214/19AOAS1269

Pena, D., and Yohai, V.J. A Fast Procedure for Outlier Diagnostics in Large Regression Problems. J. Amer. Statist. Assoc. 94 (1999). no. 446, 434–445. doi:10.2307/2670164

See Also

Other functions for initial estimates: enpy_initial_estimates(), starting_point()

regmest

Description

Compute elastic net M-estimates along a grid of penalization levels with optional penalty loadings for adaptive elastic net.

Usage

```
regmest(
 х,
 у,
  alpha,
 nlambda = 50,
  lambda,
  lambda_min_ratio,
  scale,
  starting_points,
  penalty_loadings,
  intercept = TRUE,
  cc = 4.7,
  eps = 1e-06,
  explore_solutions = 10,
 explore_tol = 0.1,
 max_solutions = 10,
  comparison_tol = sqrt(eps),
  sparse = FALSE,
  ncores = 1,
  standardize = TRUE,
  algorithm_opts = mm_algorithm_options(),
  add_zero_based = TRUE,
 mscale_bdp = 0.25,
 mscale_opts = mscale_algorithm_options()
)
```

Arguments

x	n by p matrix of numeric predictors.
У	vector of response values of length n. For binary classification, y should be a factor with 2 levels.
alpha	elastic net penalty mixing parameter with $0 \le \alpha \le 1$. alpha = 1 is the LASSO penalty, and alpha = 0 the Ridge penalty.
nlambda	number of penalization levels.
lambda	optional user-supplied sequence of penalization levels. If given and not NULL, nlambda and lambda_min_ratio are ignored.

lambda_min_ratio		
	Smallest value of the penalization level as a fraction of the largest level (i.e., the smallest value for which all coefficients are zero). The default depends on the sample size relative to the number of variables and alpha. If more observations than variables are available, the default is $1e-3 * alpha$, otherwise $1e-2 * alpha$.	
<pre>scale starting_points</pre>	fixed scale of the residuals.	
	a list of staring points, created by starting_point(). The starting points are shared among all penalization levels.	
penalty_loading		
	a vector of positive penalty loadings (a.k.a. weights) for different penalization of each coefficient. Only allowed for $alpha > 0$.	
intercept	include an intercept in the model.	
сс	cutoff constant for Tukey's bisquare ρ function.	
eps	numerical tolerance.	
explore_solutio	ns	
	number of solutions to compute up to the desired precision eps.	
explore_tol	numerical tolerance for exploring possible solutions. Should be (much) looser than eps to be useful.	
<pre>max_solutions</pre>	only retain up to max_solutions unique solutions per penalization level.	
comparison_tol	numeric tolerance to determine if two solutions are equal. The comparison is first done on the absolute difference in the value of the objective function at the solution. If this is less than comparison_tol, two solutions are deemed equal if the squared difference of the intercepts is less than comparison_tol and the squared L_2 norm of the difference vector is less than comparison_tol.	
sparse	use sparse coefficient vectors.	
ncores	number of CPU cores to use in parallel. By default, only one CPU core is used. Not supported on all platforms, in which case a warning is given.	
standardize	logical flag to standardize the x variables prior to fitting the M-estimates. Coef- ficients are always returned on the original scale. This can fail for variables with a large proportion of a single value (e.g., zero-inflated data). In this case, either compute with standardize = FALSE or standardize the data manually.	
algorithm_opts	options for the MM algorithm to compute estimates. See $mm_algorithm_options()$ for details.	
add_zero_based	also consider the 0-based regularization path in addition to the given starting points.	
<pre>mscale_bdp, msca</pre>	options for the M-scale estimate used to standardize the predictors (if $\texttt{standardize}$	
	= TRUE).	

Value

a list-like object with the following items

regmest_cv

alpha the sequence of alpha parameters.

lambda a list of sequences of penalization levels, one per alpha parameter.

scale the used scale of the residuals.

estimates a list of estimates. Each estimate contains the following information:

intercept intercept estimate.

beta beta (slope) estimate.

lambda penalization level at which the estimate is computed.

alpha *alpha* hyper-parameter at which the estimate is computed.

objf_value value of the objective function at the solution.

statuscode if > 0 the algorithm experienced issues when computing the estimate.

- status optional status message from the algorithm.
- call the original call.

See Also

regmest_cv() for selecting hyper-parameters via cross-validation. coef.pense_fit() for extracting coefficient estimates. plot.pense_fit() for plotting the regularization path. Other functions to compute robust estimates: pense()

regmest_cv Cross-validation for (Adaptive) Elastic Net M-Estimates

Description

Perform (repeated) K-fold cross-validation for regmest().

adamest_cv() is a convenience wrapper to compute adaptive elastic-net M-estimates.

Usage

```
regmest_cv(
    x,
    y,
    standardize = TRUE,
    lambda,
    cv_k,
    cv_repl = 1,
    cv_metric = c("tau_size", "mape", "rmspe", "auroc"),
    fit_all = TRUE,
    cl = NULL,
    ...
)
```

adamest_cv(x, y, alpha, alpha_preliminary = 0, exponent = 1, ...)

Arguments

x	n by p matrix of numeric predictors.
у	vector of response values of length n. For binary classification, y should be a factor with 2 levels.
standardize	whether to standardize the x variables prior to fitting the PENSE estimates. Can also be set to "cv_only", in which case the input data is not standardized, but the training data in the CV folds is scaled to match the scaling of the input data. Coefficients are always returned on the original scale. This can fail for variables with a large proportion of a single value (e.g., zero-inflated data). In this case, either compute with standardize = FALSE or standardize the data manually.
lambda	optional user-supplied sequence of penalization levels. If given and not NULL, nlambda and lambda_min_ratio are ignored.
cv_k	number of folds per cross-validation.
cv_repl	number of cross-validation replications.
cv_metric	either a string specifying the performance metric to use, or a function to eval- uate prediction errors in a single CV replication. If a function, the number of arguments define the data the function receives. If the function takes a single argument, it is called with a single numeric vector of prediction errors. If the function takes two or more arguments, it is called with the predicted values as first argument and the true values as second argument. The function must al- ways return a single numeric value quantifying the prediction performance. The order of the given values corresponds to the order in the input data.
fit_all	If TRUE, fit the model for all penalization levels. Can also be any combination of "min" and "{x}-se", in which case only models at the penalization level with smallest average CV accuracy, or within {x} standard errors, respectively. Setting fit_all to FALSE is equivalent to "min". Applies to all alpha value.
cl	a parallel cluster. Can only be used in combination with ncores = 1.
	Arguments passed on to regmest
	scale fixed scale of the residuals.
	nlambda number of penalization levels.
	<pre>lambda_min_ratio Smallest value of the penalization level as a fraction of the largest level (i.e., the smallest value for which all coefficients are zero). The default depends on the sample size relative to the number of variables and alpha. If more observations than variables are available, the default is 1e-3 * alpha, otherwise 1e-2 * alpha.</pre>
	penalty_loadings a vector of positive penalty loadings (a.k.a. weights) for different penalization of each coefficient. Only allowed for alpha > 0.
	<pre>starting_points a list of staring points, created by starting_point(). The starting points are shared among all penalization levels.</pre>
	intercept include an intercept in the model.
	add_zero_based also consider the 0-based regularization path in addition to the given starting points.
	cc cutoff constant for Tukey's bisquare ρ function.
	eps numerical tolerance.

		explore_solutions number of solutions to compute up to the desired preci- sion eps.
		explore_tol numerical tolerance for exploring possible solutions. Should be (much) looser than eps to be useful.
		<pre>max_solutions only retain up to max_solutions unique solutions per penal- ization level.</pre>
		comparison_tol numeric tolerance to determine if two solutions are equal. The comparison is first done on the absolute difference in the value of the objective function at the solution. If this is less than comparison_tol, two solutions are deemed equal if the squared difference of the intercepts is less than comparison_tol and the squared L_2 norm of the difference vector is less than comparison_tol.
		sparse use sparse coefficient vectors.
		ncores number of CPU cores to use in parallel. By default, only one CPU core is used. Not supported on all platforms, in which case a warning is given.
		<pre>algorithm_opts options for the MM algorithm to compute estimates. See mm_algorithm_options() for details.</pre>
		<pre>mscale_bdp,mscale_opts options for the M-scale estimate used to standard- ize the predictors (if standardize = TRUE).</pre>
	alpha	elastic net penalty mixing parameter with $0 \le \alpha \le 1$. alpha = 1 is the LASSO penalty, and alpha = 0 the Ridge penalty.
alpha_preliminary		
		alpha parameter for the preliminary estimate.
	exponent	the exponent for computing the penalty loadings based on the preliminary esti- mate.

Details

The built-in CV metrics are

"tau_size" τ -size of the prediction error, computed by tau_size() (default).

"mape" Median absolute prediction error.

- "rmspe" Root mean squared prediction error.
- "auroc" Area under the receiver operator characteristic curve (actually 1 AUROC). Only sensible for binary responses.

adamest_cv() is a convenience wrapper which performs 3 steps:

- 1. compute preliminary estimates via regmest_cv(..., alpha = alpha_preliminary),
- computes the penalty loadings from the estimate beta with best prediction performance by adamest_loadings = 1 / abs(beta)^exponent, and
- 3. compute the adaptive PENSE estimates via regmest_cv(..., penalty_loadings = adamest_loadings).

Value

a list-like object as returned by regmest(), plus the following components:

cvres data frame of average cross-validated performance.

a list-like object as returned by adamest_cv() plus the following components:

exponent value of the exponent.

preliminary CV results for the preliminary estimate.

penalty_loadings penalty loadings used for the adaptive elastic net M-estimate.

See Also

regmest() for computing regularized S-estimates without cross-validation.

coef.pense_cvfit() for extracting coefficient estimates.

plot.pense_cvfit() for plotting the CV performance or the regularization path. Other functions to compute robust estimates with CV: pense_cv(), pensem_cv() Other functions to compute robust estimates with CV: pense_cv(), pensem_cv()

Examples

```
# Compute the adaptive PENSE regularization path for Freeny's
# revenue data (see ?freeny)
data(freeny)
x <- as.matrix(freeny[ , 2:5])</pre>
## Either use the convenience function directly ...
set.seed(123)
ada_convenience <- adapense_cv(x, freeny$y, alpha = 0.5,</pre>
                                cv_repl = 2, cv_k = 4)
## ... or compute the steps manually:
# Step 1: Compute preliminary estimates with CV
set.seed(123)
preliminary_estimate <- pense_cv(x, freeny$y, alpha = 0,</pre>
                                  cv_repl = 2, cv_k = 4)
plot(preliminary_estimate, se_mult = 1)
# Step 2: Use the coefficients with best prediction performance
# to define the penalty loadings:
prelim_coefs <- coef(preliminary_estimate, lambda = 'min')</pre>
pen_loadings <- 1 / abs(prelim_coefs[-1])</pre>
# Step 3: Compute the adaptive PENSE estimates and estimate
# their prediction performance.
set.seed(123)
ada_manual <- pense_cv(x, freeny$y, alpha = 0.5,</pre>
                        cv_repl = 2, cv_k = 4,
                        penalty_loadings = pen_loadings)
```

residuals.pense_cvfit

```
# Visualize the prediction performance and coefficient path of
# the adaptive PENSE estimates (manual vs. automatic)
def.par <- par(no.readonly = TRUE)
layout(matrix(1:4, ncol = 2, byrow = TRUE))
plot(ada_convenience$preliminary)
plot(preliminary_estimate)
plot(ada_convenience)
plot(ada_manual)
par(def.par)
```

residuals.pense_cvfit Extract Residuals

Description

Extract residuals from a PENSE (or LS-EN) regularization path with hyper-parameters chosen by cross-validation.

Usage

```
## S3 method for class 'pense_cvfit'
residuals(
   object,
   alpha = NULL,
   lambda = "min",
   se_mult = 1,
   exact = deprecated(),
   correction = deprecated(),
   ...
)
```

Arguments

object	PENSE with cross-validated hyper-parameters to extract coefficients from.	
alpha	Either a single number or NULL (default). If given, only fits with the given alpha value are considered. If lambda is a numeric value and object was fit with multiple <i>alpha</i> values and no value is provided, the first value in object\$alpha is used with a warning.	
lambda	either a string specifying which penalty level to use ("min", "se", "{m}-se") or a single numeric value of the penalty parameter. See details.	
se_mult	It If lambda = "se", the multiple of standard errors to tolerate.	
exact	deprecated. Always gives a warning if lambda is not part of the fitted sequence and coefficients are interpolated.	
correction	defunct.	
	. currently not used.	

a numeric vector of residuals for the given penalization level.

Hyper-parameters

If lambda = "{m}-se" and object contains fitted estimates for every penalization level in the sequence, use the fit the most parsimonious model with prediction performance statistically indistinguishable from the best model. This is determined to be the model with prediction performance within $m \star cv_se$ from the best model. If lambda = "se", the multiplier *m* is taken from se_mult.

By default all *alpha* hyper-parameters available in the fitted object are considered. This can be overridden by supplying one or multiple values in parameter alpha. For example, if lambda = "1-se" and alpha contains two values, the "1-SE" rule is applied individually for each alpha value, and the fit with the better prediction error is considered.

In case lambda is a number and object was fit for several *alpha* hyper-parameters, alpha must also be given, or the first value in object\$alpha is used with a warning.

See Also

Other functions for extracting components: coef.pense_cvfit(), coef.pense_fit(), predict.pense_cvfit(),
predict.pense_fit(), residuals.pense_fit()

Examples

```
# Compute the LS-EN regularization path for Freeny's revenue data
# (see ?freeny)
data(freeny)
x <- as.matrix(freeny[ , 2:5])</pre>
regpath <- elnet(x, freeny$y, alpha = 0.75)</pre>
# Predict the response using a specific penalization level
predict(regpath, newdata = freeny[1:5, 2:5],
        lambda = regpath$lambda[[1]][[10]])
# Extract the residuals at a certain penalization level
residuals(regpath, lambda = regpath$lambda[[1]][[5]])
# Select penalization level via cross-validation
set.seed(123)
cv_results <- elnet_cv(x, freeny$y, alpha = 0.5,</pre>
                       cv_repl = 10, cv_k = 4)
# Predict the response using the "best" penalization level
predict(cv_results, newdata = freeny[1:5, 2:5])
# Extract the residuals at the "best" penalization level
residuals(cv_results)
# Extract the residuals at a more parsimonious penalization level
residuals(cv_results, lambda = "1.5-se")
```

Description

Extract residuals from a PENSE (or LS-EN) regularization path fitted by pense(), regmest() or elnet().

Usage

```
## S3 method for class 'pense_fit'
residuals(
    object,
    alpha = NULL,
    lambda,
    exact = deprecated(),
    correction = deprecated(),
    ...
)
```

Arguments

object	PENSE regularization path to extract residuals from.	
alpha	Either a single number or NULL (default). If given, only fits with the given alpha value are considered. If object was fit with multiple alpha values, and no value is provided, the first value in object\$alpha is used with a warning.	
lambda	a single number for the penalty level.	
exact	defunct Always gives a warning if lambda is not part of the fitted sequence and coefficients need to be interpolated.	
correction	defunct.	
	currently not used.	

Value

a numeric vector of residuals for the given penalization level.

See Also

Other functions for extracting components: coef.pense_cvfit(), coef.pense_fit(), predict.pense_cvfit(),
predict.pense_fit(), residuals.pense_cvfit()

Examples

```
# Compute the LS-EN regularization path for Freeny's revenue data
# (see ?freeny)
data(freeny)
x <- as.matrix(freeny[ , 2:5])</pre>
regpath <- elnet(x, freeny$y, alpha = 0.75)</pre>
# Predict the response using a specific penalization level
predict(regpath, newdata = freeny[1:5, 2:5],
        lambda = regpath$lambda[[1]][[10]])
# Extract the residuals at a certain penalization level
residuals(regpath, lambda = regpath$lambda[[1]][[5]])
# Select penalization level via cross-validation
set.seed(123)
cv_results <- elnet_cv(x, freeny$y, alpha = 0.5,</pre>
                       cv_repl = 10, cv_k = 4)
# Predict the response using the "best" penalization level
predict(cv_results, newdata = freeny[1:5, 2:5])
# Extract the residuals at the "best" penalization level
residuals(cv_results)
# Extract the residuals at a more parsimonious penalization level
residuals(cv_results, lambda = "1.5-se")
```

rho_function List Available Rho Functions

Description

List Available Rho Functions

Usage

```
rho_function(rho)
```

Arguments rho

the name of the ρ function to check for existence.

Value

if rho is missing returns a vector of supported ρ function names, otherwise the internal integer representation of the ρ function.

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starting_point

See Also

Other miscellaneous functions: consistency_const()

starting_point Create Starting Points for the PENSE Algorithm

Description

Create a starting point for starting the PENSE algorithm in pense(). Multiple starting points can be created by combining starting points via c(starting_point_1, starting_point_2, ...).

Usage

```
starting_point(beta, intercept, lambda, alpha)
as_starting_point(object, specific = FALSE, ...)
## S3 method for class 'enpy_starting_points'
as_starting_point(object, specific = FALSE, ...)
## S3 method for class 'pense_fit'
as_starting_point(object, specific = FALSE, alpha, lambda, ...)
## S3 method for class 'pense_cvfit'
as_starting_point(
    object,
    specific = FALSE,
    alpha,
    lambda = c("min", "se"),
    se_mult = 1,
    ...
)
```

Arguments

beta	beta coefficients at the starting point. Can be a numeric vector, a sparse vector of class dsparseVector, or a sparse matrix of class dgCMatrix with a single column.	
intercept	intercept coefficient at the starting point.	
lambda	optionally either a string specifying which penalty level to use ("min" or "se") or a numeric vector of the penalty levels to extract from object. Penalization levels not present in object are ignored with a warning. If NULL, all estimates in object are extracted. If a numeric vector, alpha must be given and a single number.	
alpha	optional value for the alpha hyper-parameter. If given, only estimates with matching alpha values are extracted. Values not present in object are ignored with a warning.	

object	an object with estimates to use as starting points.	
specific	whether the estimates should be used as starting points only at the penalization level they are computed for. Defaults to using the estimates as starting points f all penalization levels.	
	further arguments passed to or from other methods.	
se_mult	t If lambda = "se", the multiple of standard errors to tolerate.	

Details

A starting points can either be *shared*, i.e., used for every penalization level PENSE estimates are computed for, or *specific* to one penalization level. To create a specific starting point, provide the penalization parameters lambda and alpha. If lambda or alpha are missing, a shared starting point is created. Shared and specific starting points can all be combined into a single list of starting points, with pense() handling them correctly. Note that specific starting points will lead to the lambda value being added to the grid of penalization levels. See pense() for details.

Starting points computed via enpy_initial_estimates() are by default *shared* starting points but can be transformed to *specific* starting points via as_starting_point(..., specific = TRUE).

When creating starting points from cross-validated fits, it is possible to extract only the estimate with best CV performance (lambda = "min"), or the estimate with CV performance statistically indistinguishable from the best performance (lambda = "se"). This is determined to be the estimate with prediction performance within se_mult * cv_se from the best model.

Value

an object of type starting_points to be used as starting point for pense().

See Also

Other functions for initial estimates: enpy_initial_estimates(), prinsens()

summary.pense_cvfit Summarize Cross-Validated PENSE Fit

Description

If lambda = "se" and object contains fitted estimates for every penalization level in the sequence, extract the coefficients of the most parsimonious model with prediction performance statistically indistinguishable from the best model. This is determined to be the model with prediction performance within se_mult $* cv_se$ from the best model.

Usage

```
## S3 method for class 'pense_cvfit'
summary(object, alpha, lambda = "min", se_mult = 1, ...)
## S3 method for class 'pense_cvfit'
print(x, alpha, lambda = "min", se_mult = 1, ...)
```

tau_size

Arguments

object, x	an (adaptive) PENSE fit with cross-validation information.	
alpha	Either a single number or missing. If given, only fits with the given alpha value are considered. If lambda is a numeric value and object was fit with multiple alpha values, the parameter alpha must not be missing.	
lambda	either a string specifying which penalty level to use ("min", "se", "{x}-se") o a single numeric value of the penalty parameter. See details.	
se_mult	If lambda = "se", the multiple of standard errors to tolerate.	
	ignored.	

See Also

prediction_performance() for information about the estimated prediction performance. coef.pense_cvfit() for extracting only the estimated coefficients.

Other functions for plotting and printing: plot.pense_cvfit(), plot.pense_fit(), prediction_performance()

tau	
Lau	size

Compute the Tau-Scale of Centered Values

Description

Compute the τ -scale without centering the values.

Usage

tau_size(x)

Arguments ×

numeric values. Missing values are verbosely ignored.

Value

the τ estimate of scale of centered values.

See Also

Other functions to compute robust estimates of location and scale: mloc(), mlocscale(), mscale()

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